Consider the following two problems:

- Problem $P_1 =$ The graph homomorphism problem into $K_6$, i.e., 6-coloring, and
- Problem $P_2 =$ The graph homomorphism problem into $G$, where $G$ is the 6-cycle plus an edge.

Give a gadget reduction from $P_1$ to $P_2$. 